BULK REFRIGERATION OF FRUITS AND VEGETABLES

PART II: COMPUTER ALGORITHM FOR HEAT LOADS AND MOISTURE LOSS

by

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 ABSTRACT

 A computer algorithm was developed which estimates the latent and sensible heat loads due to the bulk refrigeration of fruits and vegetables. The algorithm also predicts the commodity moisture loss and temperature distribution which occurs during refrigeration. Part I focused upon the thermophysical properties of commodities and the flowfield parameters which govern the heat and mass transfer from fresh fruits and vegetables. This paper, Part II, discusses the modeling methodology utilized in the current computer algorithm and describes the development of the heat and mass transfer models. Part II also compares the results of the computer algorithm to experimental data taken from the literature, and, describes a parametric study which was performed with the algorithm. In addition, this paper also reviews existing numerical models for determining the heat and mass transfer in bulk loads of fruits and vegetables.
 (Keywords: fruits; vegetables; refrigeration; heat transfer; mass transfer; transpiration; respiration; bulk load models; computer algorithms)

 1 INTRODUCTION

 This is the second part of a two-part paper that describes a computer algorithm which estimates the latent and sensible heat loads due to the bulk refrigeration of fruits and vegetables as well as the commodity moisture loss and temperature distribution during refrigeration. As discussed in Part I, this algorithm was developed as an aid to both the designer and the operator of refrigeration facilities for fruits and vegetables. Part I was devoted to the modeling treatment of those thermophysical properties of commodities and flowfield parameters which affect the heat and mass transfer from fruits and vegetables.

 This paper (Part II) discusses the modeling methodology utilized in the current computer algorithm
and describes the development of the mass and heat transfer models. Part II also compares the results of the computer algorithm to experimental data taken from the literature, and, describes a parametric study which was performed with the algorithm.

A review of the literature has revealed several existing models of the heat transfer in the bulk refrigeration of fruits and vegetables, some of these models also include mass transfer. Bakker-Arkema and Bickert (1966) developed a computational model of the cooling of fruits and vegetables in a deep bed. Their model does not take into account the effects of temperature gradient within a commodity, moisture loss, or respiration. The results of their model were compared with experimental data on sugar beets and it was found that the model predicted higher temperatures than those which actually occurred in the bulk load of sugar beets. Bakker-Arkema and Bickert attributed this difference to the model's lack of an evaporative cooling algorithm.

Baird and Gaffney (1976) developed a finite difference model to predict the heat transfer which occurs in bulk loads of fruits or vegetables. They assumed that no conduction heat transfer occurs between individual commodities, and that no mass transfer occurs between the commodities and the cooling air. The results of their numerical model were compared to experimental data for the forced cooling of oranges. The numerical and experimental data agreed well. It should be noted, however, that transpiration is not considered in this model and thus, it cannot be used to determine the latent heat load produced by fruits or vegetables stored in bulk.

A computer model was developed by Adre and Hellickson (1989) to predict the refrigeration load for apples and pears in cold storage during an entire storage season. Their model incorporates estimates of heat transmission through the building envelope, infiltration, equipment and commodity heat loads, including respiration. Adre and Hellickson report that their model compared favorably with data collected from a cold storage facility. However, it includes only an abbreviated heat transfer model and no mass
A finite difference model for the cooling of swedes (rutabagas) in a deep bed was developed by Gan and Woods (1989). Their model includes the effects of respiration, moisture loss, and evaporative cooling, as well as a provision for the temperature gradient within the commodity. The transpiration rate is modeled using a transpiration coefficient consisting of two parts: a skin mass transfer coefficient and an air film mass transfer coefficient. A Sherwood correlation, used to determine the air film mass transfer coefficient, was experimentally determined for use with swedes. Comparison of their model results with experimental data on swedes yielded favorable agreement. However, their model was not generalized to include a variety of commodities.

Talbot et al. (1990) combined the Baird and Gaffney (1976) model with a porous media flow analysis to predict the temperature response of a load of oranges contained in a carton. The predicted temperature response was compared to experimental data collected on oranges to verify the applicability of the porous media flow model. It was found that the porous media flow model results were reasonable provided that variable porosity was used in the modeling of the orange cartons. However, this model does not consider moisture loss from the commodity.

MacKinnon and Bilanski (1992) developed a finite difference model of the heat and mass transfer from beds of thin leafy vegetables, such as lettuce. Heat from respiration was included in their model and mass transfer was modeled with a transpiration coefficient consisting of a skin mass transfer coefficient and an air film mass transfer coefficient. However, both the temperature gradient within the commodity, as well as the air flow rate dependence of the heat transfer coefficient were neglected. Their model results compared reasonably well with experimental data for leaf lettuce.

From this discussion, it can be seen that these existing bulk load heat and mass transfer models are not adequate to fulfill the needs of the designers and operators of bulk refrigeration facilities. Therefore, the
current computer algorithm was developed to estimate the latent and sensible heat loads as well as the moisture loss and temperature distribution in the bulk refrigeration of fruits and vegetables. This current computer algorithm is capable of modeling a wide variety of commodities.

2 MODELING METHODOLOGY

The essence of the modeling methodology used in this investigation is described below in the context of the scenario depicted in Figure 1. This figure illustrates a one dimensional air flow pattern in which the air traverses the full length of the bulk load. Figure 2 shows detail of the computational model corresponding to this one dimensional air flow pattern within the bulk load of the commodity. In the computational model, the bulk load is represented as a porous medium composed of "commodity computational cells." The refrigerated air is modeled as "air parcels" which move through the "commodity computational cells." Figure 3 shows a flow chart of the time-stepping algorithm corresponding to this scenario.

Calculation commences with a specified initial temperature and humidity for the commodity bulk load and the air contained within it. As shown in Figure 2a, the time-stepping begins with the first refrigerated "air parcel" moving into the first "commodity computational cell." At the same time, each of the initial "air parcels" moves from its original cell into the adjacent cell, while the "air parcel" within the last "commodity computational cell" moves from the bulk load into the plenum of the refrigeration unit. Within each "commodity computational cell," the commodity surface water vapor pressure, $P_s$, and air stream water vapor pressure, $P_a$, are determined based upon the commodity surface temperature, $T_s$, the "air parcel" temperature, $T_a$, and the "air parcel's" mass fraction of water vapor, $m_f$. These vapor pressures are then used to calculate the commodity transpiration, $\dot{m}$, for the time-step, $\Delta t$. The mass fraction of water vapor in each "air parcel" is then updated to reflect the effects of transpiration. Subsequently, within each cell, the heat generation due to commodity respiration, $W$, the heat transfer from the commodity, $Q$, and the evaporative
cooling due to transpiration are calculated for the time-step. Then, within each cell, the commodity
temperature and the "air parcel" temperature are both updated to reflect the effects of the calculated
respiration, heat transfer and evaporative cooling, thus completing the calculations for this time-step.

As shown in Figure 2b, the first "air parcel" moves to the second "commodity computational cell"
and a newly refrigerated second "air parcel" moves into the first "commodity computational cell." This
second "air parcel" encounters the previously updated commodity temperature in the first "commodity
computational cell."

As the time-stepping continues, each "air parcel" traverses the entire commodity bulk load. The
mass fraction of water vapor contained in each "air parcel," when it exits the bulk load, is used to calculate
the latent heat load corresponding to that "air parcel," while its temperature is used to calculate its sensible
heat load. As this algorithm time-steps towards a steady state, an estimate of the time histories of the latent
and sensible heat loads, as well as commodity moisture loss and temperature distribution, are obtained.

3 DESCRIPTION OF THE MASS AND HEAT TRANSFER MODELS

The modeling of the mass and heat transfer, between the air and the bulk load of commodities within
a "commodity computational cell," is achieved by formulating the mass and heat transfer with respect to a
single commodity item, and then multiplying by the number of items resident within the "commodity
computational cell." The number of commodity items resident within the "commodity computational cell,"
\( n_c \), is determined by the following equation:

\[
n_c = \frac{w_{bulk}}{w_c \cdot N_{cell}}
\]

where \( w_{bulk} \) is the mass of the bulk load, \( w_c \) is the mass of a single commodity item and \( N_{cell} \) is the number of
"commodity computational cells" in the bulk load.
3.1 Mass Transfer Calculation

As discussed in Section 2.1 of Part I, the moisture loss from a single commodity item is modeled as follows:

\[ \dot{m} = k_t (P_s - P_a) \]  \hspace{1cm} (2)

where \( P_s \) is the water vapor pressure at the surface of the commodity and \( P_a \) is the water vapor pressure in the refrigerated air. Both \( P_s \) and \( P_a \) are evaluated at the previous time step by utilizing the relationships developed in Sections 3.1 through 3.3 of Part I. The transpiration coefficient, \( k_t \), is given as:

\[ k_t = \frac{1}{\frac{1}{k_a} + \frac{1}{k_s}} \]  \hspace{1cm} (3)

where \( k_a \) is the air film mass transfer coefficient and \( k_s \) is the skin mass transfer coefficient as described in Sections 2.1.1 and 2.1.2 of Part I, respectively.

For one computational cell, the transpiration rate becomes:

\[ \dot{m}_t = \dot{m} A_s n_c \]  \hspace{1cm} (4)

where \( \dot{m}_t \) is the total transpiration rate in the computational cell, \( \dot{m} \) is the transpiration rate per unit area of the commodity surface, \( A_s \) is the surface area of a single commodity item, and \( n_c \) is the number of commodities in the computational cell.

During the time step, \( \Delta t \), the mass of water vapor in the air of the computational cell increases as follows:

\[ m^1_{H_2O} = m^0_{H_2O} + \dot{m}_t \Delta t \]  \hspace{1cm} (5)

where \( m^1_{H_2O} \) is the updated mass of water vapor in the air, \( m^0_{H_2O} \) is the mass of water vapor in the air from the previous time step, \( \dot{m}_t \) is the transpiration rate and \( \Delta t \) is the time step size.
To find the mass of water vapor in the air from the previous time step, the mass fraction of the water vapor in the air from that time step must first be calculated. The mass fraction of water vapor in the air of the computational cell at the end of the previous time step, \( m_f^0 \), may be found as follows:

\[
\frac{m_f^0}{m_a^0} = \frac{w^0}{1 + w^0}
\]

(6)

where \( w^0 \) is the humidity ratio of the air from the previous time step. The mass of water vapor in the air from the previous time step then becomes:

\[
m_{H_2O}^0 = m_f^0 \cdot m_a^0
\]

(7)

where \( m_a^0 \) is the mass of the air in the computational cell at the end of the previous time step. This mass of air is given by:

\[
m_a^0 = \rho_a^0 \cdot v_a
\]

(8)

where \( \rho_a^0 \) is the density of the air at the end of the previous time step and \( v_a \) is the volume of the air in the computational cell.

The updated mass fraction of water vapor in the air of the computational cell, \( m_f^1 \), then becomes:

\[
m_f^1 = \frac{m_{H_2O}^1}{m_a^0 + m_t \cdot \Delta t}
\]

(9)

With the updated mass fraction of water vapor in the air, the new humidity ratio of the air, \( w^1 \), may be found:

\[
w^1 = \frac{m_f^1}{1 - m_f^1}
\]

(10)

This completes the transpiration calculations for one computational cell for the current time step.
3.2 Heat Transfer Calculation

In order to make the modeling of commodity heat transfer tractable, the commodities were assumed to be spherical in shape with uniform internal heat generation due to respiration. It was further assumed that the temperature within a commodity varied only in the radial direction. With these assumptions, the governing form of the transient heat equation is formally written as follows (Incropera and DeWitt, 1990):

$$\frac{k}{r^2} \frac{\partial}{\partial r} \left( r^2 \frac{\partial T}{\partial r} \right) + \rho W = \rho c \frac{\partial T}{\partial t}$$  \hspace{1cm} (11)

where \( r \) denotes the radial direction within the commodity, \( k \) is the commodity thermal conductivity, \( T \) is the commodity temperature, \( W \) is the respiratory heat generation of the commodity per unit mass, \( \rho \) is the commodity density, \( c \) is the commodity specific heat, and \( t \) is time.

An explicit finite difference technique was applied to Equation (11) by dividing a commodity into \( N \) spherical shells as shown in Figure 4. The resulting finite difference equation applicable to the center node is given as follows:

$$\frac{k A_i}{\Delta r} (T_2^0 - T_1^0) + \rho v_1 W_i = \frac{\rho c v_i (T_1^1 - T_1^0)}{\Delta t}$$  \hspace{1cm} (12)

where \( A_i \) is the area through which heat is transferred from the center node, \( \Delta r \) is the distance between nodes, \( T_2^0 \) is the temperature of the neighbor node at the previous time step, \( T_1^0 \) is the temperature of the center node at the previous time step, \( v_i \) is the volume of the center node, \( W_i \) is the heat generation per unit mass due to respiration for the center node, \( T_1^1 \) is the temperature of the center node at the current time step and \( \Delta t \) is the time step.

For the interior nodes, the finite difference equation becomes:

$$\frac{k A_{i-1}}{\Delta r} (T_{i-1}^0 - T_i^0) + \frac{k A_i}{\Delta r} (T_{i+1}^0 - T_i^0) + \rho v_i W_i = \frac{\rho c v_i (T_1^1 - T_i^0)}{\Delta t}$$  \hspace{1cm} (13)
where $A_{i-1}$ is the area through which heat is transferred from the neighbor node, $\Delta r$ is the distance between nodes, $T_{i-1}^{0}$ is the temperature of the neighbor node at the previous time step, $T_{i}^{0}$ is the temperature of the current node at the previous time step, $A_{i}$ is the area through which heat is transferred from the current node, $T_{i+1}^{0}$ is the temperature of the neighbor node at the previous time step, $W_{i}$ is the heat generation per unit mass due to respiration for the current node, $v_{i}$ is the volume of the current node and $T_{i+1}^{1}$ is the temperature of the current node at the current time step.

At the surface of the commodity, convection heat transfer, radiation heat transfer, and evaporative cooling due to transpiration must be considered. Thus, the finite difference equation at the commodity surface becomes:

$$\frac{k A_{N-1}}{\Delta r} (T_{N-1}^{0} - T_{N}^{0}) + h_{\text{eff}} A_{s} (T_{a}^{0} - T_{N}^{0}) - L \dot{m} A_{s} + \rho v_{N} W_{N} = \frac{\rho c v_{N} (T_{N}^{1} - T_{N}^{0})}{\Delta t}$$

(14)

where $A_{N-1}$ is the area through which heat is transferred from the neighbor node, $\Delta r$ is the distance between nodes, $T_{N-1}^{0}$ is the temperature of the neighbor node at the previous time step, $T_{N}^{0}$ is the temperature of the surface node at the previous time step, $A_{s}$ is the surface area of a single commodity item, $T_{a}^{0}$ is the air temperature at the previous time step, $L$ is the latent heat of vaporization for water, $\dot{m}$ is the transpiration rate per unit area of commodity surface, $v_{N}$ is the volume of the surface node and $T_{N}^{1}$ is the temperature of the surface node at the current time step.

As discussed in Section 3.9 of Part I, the effective heat transfer coefficient, $h_{\text{eff}}$, includes both convection and radiation:

$$h_{\text{eff}} = h_{\text{convection}} + h_{\text{radiation}}$$

(15)

The convection heat transfer coefficient, $h_{\text{convection}}$, is determined via a Nusselt-Reynolds-Prandtl correlation, Equation (35), given in Section 3.9.1 of Part I, while the radiation heat transfer coefficient, $h_{\text{radiation}}$, is given by Equation (39), derived in Section 3.9.2 of Part I.
The formulation given by Equations (12) through (14) defines the temperature distribution within a single commodity item. However, Equation (14) requires knowledge of the temperature of the air parcel resident within the "commodity computational cell," $T_{a0}$. This air temperature is determined at each time step by performing a heat balance between the air parcel and that portion of the bulk load which is contained within the "commodity computational cell."

$$n_c \cdot h_{eff} \cdot A_s \cdot (T_{a0} - T^{(n)}_a) = m_0 \cdot c_{p,a} \cdot \frac{(T^{(n+1)}_a - T^{(n)}_a)}{\Delta t}$$

(16)

where $n_c$ is the number of commodity items resident within the "commodity computational cell," $m_0$ is the mass of air in the computational cell and $c_{p,a}$ is the specific heat of air. This completes the formulation of the heat transfer model for one computational cell.

Since Equations (12) through (14) and (16) are explicit finite difference equations, they can be solved directly for the updated nodal temperatures. The heat transfer calculation begins at the commodity center node and proceeds outward to the air parcel. This completes the heat transfer calculation for one computational cell for the current time step.

4 EXPERIMENTAL VERIFICATION OF THE COMPUTER ALGORITHM

To verify the accuracy of the current computer algorithm, its calculated results were compared with experimental data obtained from the literature. Baird and Gaffney (1976) reported experimental data taken from bulk loads of oranges. They recorded commodity center and surface temperatures at the air exit of a bulk load for a period of two hours. The bulk load of oranges was 0.67 m (2.2 ft) deep and the commodities were initially at $32^\circ C (90^\circ F)$. The refrigerated air was at a temperature of $-1.1^\circ C (30^\circ F)$ and approached the bulk load with a velocity of 0.91 m/s (3.0 ft/s). Figure 5 shows Baird and Gaffney's experimental data along with the output from the current computer algorithm. Comparison of the model results with Baird and Gaffney's data on oranges shows that the current algorithm correctly predicts the trends of commodity
temperatures with a maximum error of 1.4°C (2.5°F).

Gan and Woods (1989) gathered experimental data on swedes (rutabagas) during cooling in a thin bed. Air at 4.96°C (40.9°F), 83.71% relative humidity flowed at a velocity of 0.53 m/s (1.7 ft/s) through a bed of swedes which was initially at a temperature of 21.7°C (71.1°F). Commodity center temperature and moisture loss were recorded for a period of eight hours. Figure 6 shows the Gan and Woods temperature data along with the output from the current algorithm, while Figure 7 shows the Gan and Woods moisture loss data along with the output from the current algorithm. It is seen that the current algorithm correctly predicts commodity temperatures within 2.2°C (4.0°F) and moisture loss within 0.38%.

Güemes et al. (1989) collected temperature data for the cooling of strawberries in a thin bed. Air with a velocity of 3.0 m/s (9.8 ft/s) and a temperature of 2.1°C (36°F) was used to cool the strawberries for a period of 16 minutes. As shown in Figure 8, the output from the current algorithm compares favorably with the data from Güemes et al. The maximum error between the computer algorithm and the experimental results was 1.9°C (3.4°F).

Brusewitz et al. (1992) conducted experiments to determine moisture loss from peaches during post-harvest cooling. The post-harvest cooling was performed at 4°C (39°F), 92% relative humidity in a chamber with 20 air changes per minute for a period of four days. Peaches were picked in the morning when the ambient temperature was 16°C (61°F). Experimental data from Brusewitz et al. shows that the peaches lost 2.5% of their weight due to moisture loss during the four day cooling period. The current computer algorithm predicted a weight loss of 2.53% at the end of the four day period, in good agreement with the experimental data. Figure 9 shows the results from the current computer algorithm as well as the experimental data.

5 PARAMETRIC STUDIES UTILIZING THE CURRENT ALGORITHM

A parametric study was performed to investigate the influence of various parameters on the
calculated cooling time and moisture loss of bulk loads of commodities. This parametric study utilized a bulk load of apples with dimensions of 1m X 1m X 2m (3.3 ft X 3.3 ft X 6.6 ft) and a bulk weight of 800 kg (1764 lb). The initial temperature of the load was taken to be 24°C (75°F). The dry bulb temperature of the refrigerated air was taken to be 1.67°C (35°F). The bulk load was divided into 5 cells and cooling was simulated for 12 hours. The effects of bulk weight, air flow rate and relative humidity on cooling time and moisture loss were investigated.

5.1 Effect of Bulk Weight on Cooling Time

Figure 10 shows the commodity center temperature versus time response at the air exit of the bulk load for bulk weights of 720 kg (1587 lb), 800 kg (1764 lb) and 880 kg (1940 lb) with an air flow rate of 0.487 m³/s (17.2 ft³/s) and a relative humidity of 89%. It can be seen that a considerable difference in the time history of commodity center temperature exists between the three bulk loads. As is expected, an increase in bulk weight results in an increase in cooling time.

5.2 Effect of Air Flow Rate on Cooling Time

Figure 11 shows the commodity center temperature versus time response at the air exit of the bulk load for air flow rates of 0.440 m³/s (15.5 ft³/s), 0.487 m³/s (17.2 ft³/s) and 0.538 m³/s (19.0 ft³/s) and a relative humidity of 89%. As shown in Figure 11, cooling time decreases with increasing air flow rate.

5.3 Effect of Air Flow Rate on Moisture Loss

As shown in Figure 12, moisture loss decreases with increasing air flow rate. This is expected, since at higher air flow rates, the cooling time is reduced. A reduction in the cooling time decreases the vapor pressure deficit more quickly, thus retarding transpiration.

5.4 Effect of Relative Humidity on Moisture Loss and Cooling Time

To study the effects of the relative humidity of the incoming refrigerated air, the air wet bulb temperature was varied from -3.3°C to 1.5°C (26°F to 34.7°F) while the air dry bulb temperature and flow
rate were held constant at 1.67°C (35°F) and 0.487 m³/s (17.2 ft³/s), respectively. This results in a relative humidity range of 20% to 97%. As shown in Figure 13, increased relative humidity results in decreased moisture loss. Such behavior is not unexpected. An increase in relative humidity causes a decrease in the vapor pressure deficit, thus decreasing transpiration. Relative humidity was found to have little or no noticeable effect upon the cooling time of the apples.

5.5 Effect of Skin Mass Transfer Coefficient on Moisture Loss and Cooling Time

For an air flow rate of 0.487 m³/s (17.2 ft³/s) and a relative humidity of 89%, the effect of the skin mass transfer coefficient, \( k_s \), on moisture loss was investigated for the bulk load of apples. As discussed in Section 2.1.2 of Part I, the computer algorithm incorporates three values of skin mass transfer coefficient for each commodity: a low value, a mean value and a high value. As shown in Figure 14, a considerable difference in moisture loss is obtained between the three values of the skin mass transfer coefficient. An increase in the skin mass transfer coefficient results in an increase in transpiration. Skin mass transfer coefficient was found to have little or no noticeable effect upon the cooling time of apples.

6 CONCLUSIONS

These papers (Part I and II) have described the development and performance of a computer algorithm which estimates the latent and sensible heat loads as well as the moisture loss and temperature distribution in the bulk refrigeration of fruits and vegetables. This algorithm, which was developed as an aid to both the designer and the operator of refrigeration facilities, is capable of modeling a wide variety of commodities. Part I focused upon the thermophysical properties of commodities and the flowfield parameters which govern the heat and mass transfer from fresh fruits and vegetables.

This paper (Part II) described the modeling methodology which was devised for studying the mass and heat transfer processes within a bulk load of commodities. In the computational model, the bulk load is represented as a porous medium composed of "commodity computational cells" and the refrigerated air is
modeled as "air parcels" which move through these "commodity computational cells." The modeling of the mass and heat transfer between the air and the bulk load is achieved by formulating the mass and heat transfer with respect to a single commodity item and then multiplying by the number of items resident within the "commodity computational cell."

A mass transfer model was developed to update the mass fraction of water vapor within each "commodity computational cell" at each time step based upon the transpiration model identified in Part I. An explicit finite difference formulation of the transient heat equation in spherical coordinates was derived which accounts for both radiation and convection heat transfer at the commodity surface. This formulation yields the temperature distribution within the commodities resident in each "commodity computational cell" at each time step. It also yields the temperature of the "air parcel" resident within each "commodity computational cell" at each time step.

To verify the accuracy of the current algorithm, its calculated results were compared with experimental data obtained from the literature. The results of the heat transfer model were compared to experimental temperature data for oranges, strawberries and swedes, while the results of the mass transfer model were compared to experimental moisture loss data for swedes and peaches. The results of these comparisons show good agreement between the numerical results and the experimental data for both temperature and moisture loss.

Utilizing the current computer algorithm, a parametric study was performed to investigate the influence of bulk weight, air flow rate, skin mass transfer coefficient and relative humidity upon the cooling time and moisture loss of a bulk load of apples. It was found that relative humidity and skin mass transfer coefficient had little effect on cooling time while bulk weight and air flow rate where of primary importance to cooling time. Moisture loss was found to vary appreciably with relative humidity, air flow rate and skin mass transfer coefficient while bulk weight had little effect. It is noteworthy that an increase in air flow rate
results in a decrease in moisture loss. The increased air flow rate reduces the cooling time which quickly reduces the vapor pressure deficit, thus lowering the transpiration rate.

**NOMENCLATURE**

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<td>$A_i$</td>
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<td>$A_s$</td>
<td>single commodity surface area</td>
</tr>
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<td>$c$</td>
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\( t \)  
- time

\( T \)  
- commodity temperature

\( T_a \)  
- dry bulb air temperature

\( T_a^0 \)  
- air temperature at time \( t \)

\( T_a^1 \)  
- air temperature at time \( t + \Delta t \)

\( T_i^0 \)  
- temperature of \( i^{th} \) node at time \( t \)

\( T_i^1 \)  
- temperature of \( i^{th} \) node at time \( t + \Delta t \)

\( T_N^0 \)  
- temperature of surface node at time \( t \)

\( T_N^1 \)  
- temperature of surface node at time \( t + \Delta t \)

\( T_s \)  
- product surface temperature

\( T_1^0 \)  
- temperature of center node at time \( t \)

\( T_1^1 \)  
- temperature of center node at time \( t + \Delta t \)

\( v_a \)  
- volume of air in computational cell

\( v_i \)  
- volume of \( i^{th} \) node

\( v_N \)  
- volume of surface node

\( v_1 \)  
- volume of center node

\( w^0 \)  
- humidity ratio at time \( t \)

\( w^1 \)  
- humidity ratio at time \( t + \Delta t \)

\( w_{\text{bulk}} \)  
- mass of bulk load

\( w_c \)  
- mass of single commodity

\( W \)  
- rate of respiratory heat generation of commodity per unit mass of commodity

\( W_i \)  
- rate of respiratory heat generation of commodity per unit mass of commodity for node \( i \)

\( W_1 \)  
- rate of respiratory heat generation of commodity per unit mass of commodity for center node

\( \Delta r \)  
- length of node in radial direction

\( \Delta t \)  
- time step size

\( \rho \)  
- density of commodity

\( \rho_a^0 \)  
- density of air at time \( t \)
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REFERENCES


Figure 1. Refrigerated bulk storage of fruits and vegetables.
Figure 2. Computational model of refrigerated air flow through bulk load of commodity.
Figure 3. Flow chart of time-stepping algorithm.
Figure 4. Commodity grid.
Figure 5. Current numerical results and experimental temperature data for forced air cooling of oranges from Baird and Gaffney (1976). The approaching air temperature and velocity were -1.1°C and 0.91 m/s, respectively.

Figure 6. Current numerical results and experimental temperature data for forced air cooling of swedes from Gan and Woods (1989). The approaching air temperature, relative humidity and velocity were 4.96°C, 83.71%, and 0.53 m/s, respectively.
Figure 7. Current numerical results and experimental moisture loss data for forced air cooling of swedes from Gan and Woods (1989). The approaching air temperature, relative humidity and velocity were 4.96°C, 83.71%, and 0.53 m/s, respectively.

Figure 8. Current numerical results and experimental temperature data for forced air cooling of strawberries from Güemes et al. (1989). The approaching air temperature and velocity were 2.1°C and 3.0 m/s, respectively.
Figure 9. Current numerical results and experimental moisture loss data for post harvest cooling of peaches from Brusewitz et al. (1992). Cooling was performed at 4.0°C, 92% relative humidity with 20 air changes per minute.

Figure 10. Effect of bulk weight on the forced air cooling time of apples located at the air exit of the bulk load. The approaching air temperature, humidity and flow rate were 1.67°C, 89%, and 0.487 m³/s, respectively.
Figure 11. Effect of air flow rate on the forced air cooling time of apples located at the air exit of the bulk load. The approaching air temperature and humidity were 1.67°C and 89%, respectively.

Figure 12. Effect of air flow rate on moisture loss. The approaching air temperature and humidity were 1.67°C and 89%, respectively.
Figure 13. Effect of relative humidity on moisture loss. The approaching air temperature and flow rate were 1.67°C and 0.487 m³/s, respectively.

Figure 14. Effect of skin mass transfer coefficient on moisture loss. The approaching air temperature, humidity and flow rate were 1.67°C, 89%, and 0.487 m³/s, respectively.